Seeking Interpretability and Explainability in Binary Activated Neural Networks

Benjamin Leblanc, Pascal Germain

August 31st, 2023

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We define the degree of interpretability

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We define the degree of interpretability of a predictor

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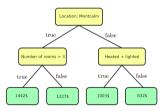
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We define the degree of interpretability of a predictor by the capacity of a non-expert to understand its decision process solely by considering the model in itself.

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 $\hat{y} = 70\$ +$

90¢ \times number of square foot + 58\$ \times number of rooms

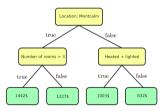


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• Additive model



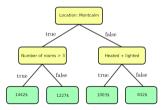
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- Additive model
- Simple interactions between features

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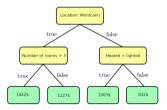


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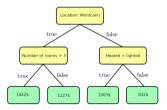


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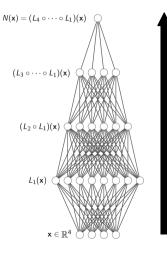
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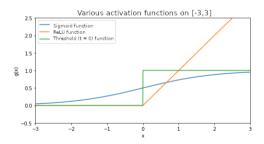
• Here : fully connected neural networks

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- $B(\mathbf{x}) = (L_1 \circ \cdots \circ L_1)(\mathbf{x}) = L_1(\ldots L_2(L_1(\mathbf{x}))\ldots)$

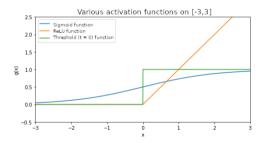
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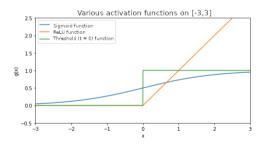




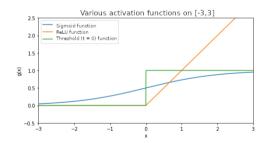
• Savings on computing time



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- Predictors are less prone to overfitting [1-2]



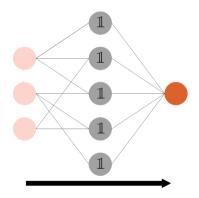
- Savings on computing time
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- Interpretability possibilities



Simple neural networks

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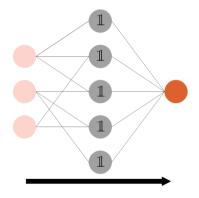
Simple neural networks



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Simple neural networks

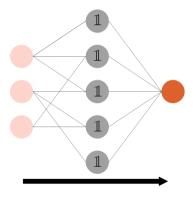
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Simple neural networks

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$$\mathbb{1}_{\{x\}} = egin{cases} 1 & ext{if } x \geq 0, \\ 0 & ext{otherwise.} \end{cases}$$

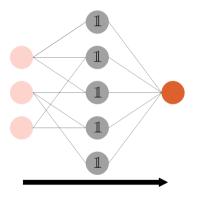


Simple neural networks

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• Shallow networks (1 hidden layer)

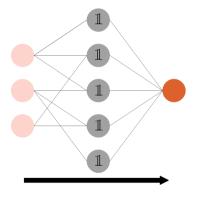


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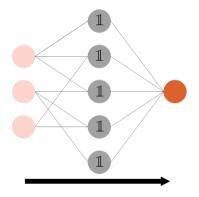


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- Sparse (2)



Characteristics

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- No hyperparameter (learning rate, batch size, ...)

SHAP values

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• Goal: quantifying the contribution (magnitude, impact) of each feature to a prediction

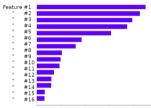
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SHAP values

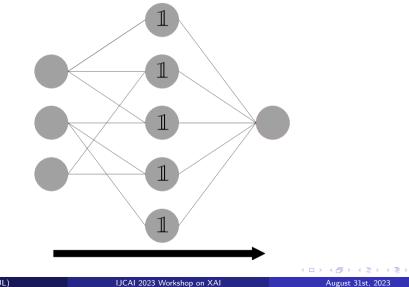
- Goal: quantifying the contribution (magnitude, impact) of each feature to a prediction
- At a prediction or a dataset level of aggregation

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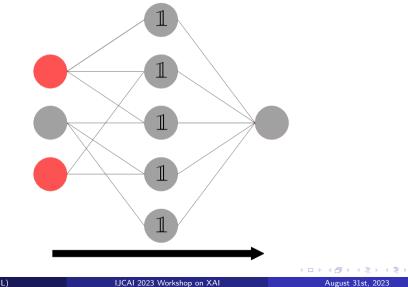
average impact on model output magnitude



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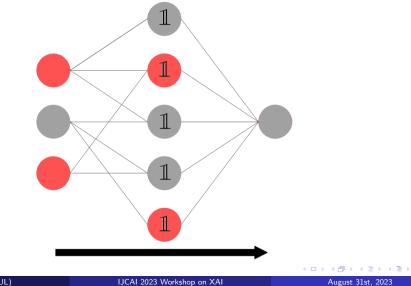
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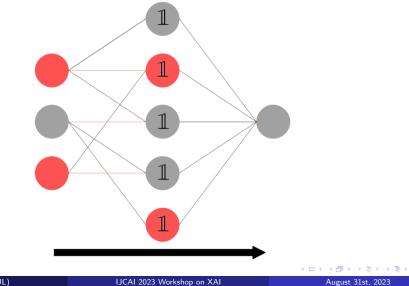
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Algorithm 1-BANN SHAP

1: Input : { x_1, \ldots, x_m }, $x \in \mathbb{R}^d$, the features of dataset 2: B, a BANN; $\{\mathbf{W}_1, \ldots, \mathbf{W}_l\}$, its weights 3: **R** = $\mathbf{0}_{d \times d \times |L_1|}$ 4: $C = 0_{1 \times d}$ 5: For $g \in \{1, \ldots, |L_1|\}$: 6: $\mathbf{a} = \mathbb{1}_{\{\mathbf{w}_{\sigma} \neq 0\}}$ 7. $\mathbf{C} = \mathbf{C} \cup comb(\mathbf{a})$ 8: For $i \in \{1, ..., d\}$ such that $(\exists i \mid c_{i,i} = 1)$: Q٠ For $i \in \{1, ..., |\mathbf{C}|\}$ such that $c_{i,i} = 1$: For $\mathbf{x}, \mathbf{x}' \in S$: 10: If $L_1\left(\mathbf{x}_{\mathbf{c}\setminus\{f\}}\cup\mathbf{x}'_{\overline{\mathbf{c}\setminus\{f\}}}\right)\neq L_1(\mathbf{x}_{\mathbf{c}}\cup\mathbf{x}'_{\overline{\mathbf{c}}})$: 11: $\mathbf{r}_{i,|c_{i,i}|_1} = \mathbf{r}_{i,|c_{i,i}|_1} + \frac{\theta_{\mathbf{x},f}}{m} \odot \left| \sum_{k=1}^{d_i} \mathbf{w}_k \right|,$ 12: 13: with $\theta_{\mathbf{x},f} = \left| L_1\left(\mathbf{x}_{\mathbf{c} \setminus \{f\}} \cup \mathbf{x}_{\overline{\mathbf{c}} \setminus \{f\}} \right) - L_1(\mathbf{x}_{\mathbf{c}} \cup \mathbf{x}_{\overline{\mathbf{c}}}) \right|$ 14: Return R

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The task

• Task: predict the cost of a house (measured in 100k USD)

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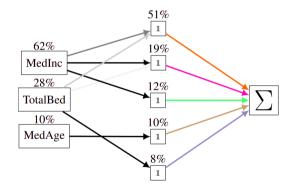
$$\begin{split} B(\text{MedInc, MedAge, TotalBed}) &= \\ 1.00 + \\ 1.27 \cdot \mathbb{1}_{\{0.08 \cdot \text{TotalBed} + \text{MedInc} > 65.46\}} + \\ 1.01 \cdot \mathbb{1}_{\{0.59 \cdot \text{TotalBed} + \text{MedInc} > 63.56\}} + \\ 0.60 \cdot \mathbb{1}_{\{\text{MedInc} > 28.20\}} + \\ 0.36 \cdot \mathbb{1}_{\{\text{TotalBed} > 622.0\}} + \\ 0.27 \cdot \mathbb{1}_{\{\text{MedAge} > 20.0\}} \end{split}$$

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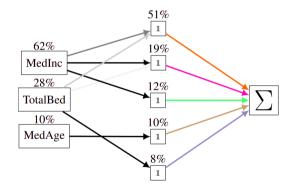
The criterion

- Additive model
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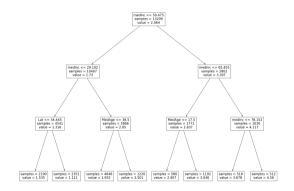
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Artificial neural networks can be interpretable predictors...

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Artificial neural networks can be interpretable predictors...

... When trained with such a goal in mind!

Benjamin Leblanc (UL)

[1] J. Lin, C. Gan, and S. Han, "Defensive quantization: When efficiency meets robustness," CoRR, vol. abs/1904.08444, 2019.

[2] M. Courbariaux, I. Hubara, D. Soudry, R. El-Yaniv, and Y. Bengio, "Binarized neural networks: Training deep neural networks with weights and activations constrained to +1 or -1," 2016.

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Thank you for your attention :)